Solution

Class 10 - Mathematics

2020-2021 - Paper-7

Part-A

1. We know that HCF of two numbers is a divisor of their LCM. Here, 18 is not a divisor of 380. But 380 = 18×21+2

Here 2 is remainder so 380 is not divisible by 18.

So, 18 and 380 cannot be respectively HCF and LCM of two numbers.

OR

Since the decimal expansion is non-terminating but recurring, the given number is a rational number of the form $\frac{p}{q}$ and q is not of the form $2^{m} \times 5^{n}$ that is, the prime factors of q will also have a factor other than 2 and 5.

2. Given, $2x^2 - 2\sqrt{2}x + 1 = 0$ Here, $a = 2, b = -2\sqrt{2}, c = 1$. So, $b^2 - 4ac = 8 - 8 = 0$ Therefore, $x = \frac{2\sqrt{2}\pm\sqrt{0}}{4} = \frac{\sqrt{2}}{2} \pm 0$ i.e., $x = \frac{1}{\sqrt{2}}$ So, the roots are $\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}$ 3. The given pair of linear equations x - 2y - 8 = 0and 5x - 10y - c = 0On Comparing with ax + by + c = 0; Here, $a_1 = 1, b_1 = -2, c_1 = -8$; And $a_2 = 5, b_2 = -10, c_2 = -c$; $a_1/a_2 = 1/5$ $b_1/b_2 = 1/5$ $c_1/c_2 = 8/c$

But if c = 40 (real value), then the ratio c_1/c_2 becomes 1/5 and then the system of linear equations has an infinitely many solutions.

Hence, at c= 40, the system of linear equations does not have a unique solution.

4. ∵ BD is a diameter

 $\therefore \angle BCD = 90^{\circ}$ [Angle in the semi-circle]

 $\therefore \angle BCP = 180^{\circ} - 90^{\circ} - 40^{\circ} = 50^{\circ}$

5. Here,

 $a_n = n^2 + 1$ So, $a_1 = 1^2 + 1 = 2$ $a_2 = 2^2 + 1 = 5$ $a_3 = 3^2 + 1 = 10$ List of numbers becomes 2, 5, 10,..... Here, $5 - 2 \neq 10$ -5, so it does not form an A.P.

OR

0.6, 1.7, 2.8, 3.9... First term = a= 0.6 Common difference (d) = Second term -First term = Third term - Second term and so on Therefore, Common difference (d) = 1.7–0.6=1.1 6. $\frac{1}{3}, \frac{5}{3}, \frac{9}{3}, \frac{13}{3}, \dots$ First term (a) = $\frac{1}{3}$ Common difference (d) = $\frac{5}{3} - \frac{1}{3} = \frac{4}{3}$ 7. Given (x + 4)² - 8x = 0 $\Rightarrow x^2 + 8x + 16 - 8x = 0$ $\therefore x^2 + 16 = 0$ $\therefore D = b^2 - 4ac = (0) - 4(1) (16) < 0$ Hence, the equation (x + 4)² - 8x = 0 has no real roots.

OR

We have given that $x^2 + 4x + 5 = 0$. Here, a = 1, b = 4, c = 5. So, $b^2 - 4ac = 16 - 20 = -4 < 0$. Since the square of a real number cannot be negative, therefore $\sqrt{b^2 - 4ac}$ will not have any real value. So, there are no real roots for the given equation.



Consider C is an external point as shown in figure.

According to theorem, from an external point only two tangents can be drawn to a circle. So, value of k = 2

9. PA and PB are two tangents drawn from an external point P to a circle.



OR

Given , A line touches a circle of radius 4 cm. Distance between two parallel tangents = Diameter of the circle = $2 \times 4 = 8$ cm.

10. $riangle AHK \sim \Delta ABC$

$$\Rightarrow \frac{AK}{AC} = \frac{HK}{BC}$$
$$\Rightarrow \frac{10}{x} = \frac{7}{3.5}, \text{ when AC} = x \text{ cm}$$
$$\Rightarrow x = \frac{10 \times 3.5}{7} = 5$$

 \therefore AC = 5 cm.

11. We have $a_1 = -1$, $a_2 = -1$, $a_3 = -1$ and $a_4 = -1$

a₂ - a₁ = 0

a₃ - a₂ = 0

$$a_4 - a_3 = 0$$

Clearly, the difference of successive terms is same, therefore given list of numbers form an AP. $\tan 26^\circ$

12. We have $\frac{\tan 26^{\circ}}{\cot 64^{\circ}}$ by using $\tan(90^{\circ} - A) = \cot A$, we get $= \frac{\tan(90^\circ - 64^\circ)}{\cot 64^\circ}$ = $\frac{\cot 64^\circ}{\cot 64^\circ}$ = 1 13. $\tan A = \frac{3}{4}$ and $A + B = 90^\circ \Rightarrow B = 90^\circ - A$ $\therefore \cot B = \cot(90^\circ - A) = \tan A$ = $\frac{3}{4}$ 14. Edge of the cube = 4.2 cm Diameter of base of cone=4.2 cm Radius = $\frac{4.2}{2}$ = 2.1 cm

- 15. Given AP: 75, 67, 59, 51,... Common difference = 67 - 75 = -8 5th term = 51 - 8 = 43 6th term = 43 - 8 = 35
- 16. After removing king, queen and jack of clubs from a deck of 52 playing cards there are 49 cards left in the deck. Out of these 49 cards one card can be chosen in 49 ways.

There are 13 heart cards in the deck containing 49 cards out of which one heart card can be chose in 13 ways. .:. Favourable number of elementary events = 13

Hence, P (Getting a heart) = $\frac{13}{49}$

OR

No, the outcomes are not equally likely, because 3 contains half part of the total region, so it is more likely than 1 and 2, since 1 and 2, each contains half part of the remaining part of the region.

- 17. i. (d) The perpendiculars from P, Q, R and S intersect the x-axis at 3, 10, 10 and 3 respectively. Also, the perpendiculars from P, Q, R and S intersect the y-axis at 6, 6, 2, 2 respectively. Hence coordinates of P and S are: P(3, 6) and S(3, 2).
 - ii. (b) Let M be the mid-point of QS. So using mid-point formula, Coordinates of M are $(\frac{3+10}{2}, \frac{2+6}{2}) = (\frac{13}{2}, 4)$

iii. (a) Now, PQ =
$$\sqrt{(10-3)^2 + (6-6)^2} = \sqrt{49} = 7 \text{ m}$$

PS = $\sqrt{(3-3)^2 + (2-6)^2} = \sqrt{16} = 4 \text{ m}$

Hence, area of rectangle PQRS = PQ \times PS = 7 \times 4 = 28 m²

iv. (c) R(10, 2), Q(10, 6)

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v. (b) 7, 4
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- 18. i. (c) 90⁰
 - ii. (b) SAS
 - iii. (b) 4:9
 - iv. (d) Converse of Pythagoras theorem
 - v. (a) 48 cm²
- 19. i. (a) 46-48
 - ii. (b) 46.9 kg
 - iii. (a) Mean
 - iv. (c) 45.85
 - v. (b) 14K

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20. i. (a) 196.25 cm<sup>3</sup>
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- ii. (b) 32.71 cm³
- iii. (c) 163.54 cm³
- iv. (b) 9.81 cm³
- v. (d) 186.44 cm³

Part-B

21. Let us assume, to the contrary, that $3\sqrt{2}$ is rational. That is, we can find coprimes a and b (b ≠ 0) such that $3\sqrt{2} = \frac{a}{L}$ Rearranging, we get $\sqrt{2} = rac{a}{3b}$...(i) Since 3, a and b are integers, $\frac{a}{3b}$ is rational, and so (i) shows that $\sqrt{2}$ is rational. But this contradicts the fact that $\sqrt{2}$ is irrational. So, we conclude that $3\sqrt{2}$ is irrational. 22. Since (a, b) is the mid-point of the line segment A(10, -6) and B(k, 4), $a=rac{10+k}{2}$ and b = $rac{-6+4}{2}$ \Rightarrow 2a = 10 + k and $b = \frac{-2}{2}$ \Rightarrow k = 2a - 10 and b = -1 Now, a - 2b = 18 \Rightarrow a - 2(-1) = 18 \Rightarrow a + 2 = 18 \Rightarrow a = 16 Hence, $k = 2 \times 16 - 10 = 32 - 10 = 22$ $\therefore AB = \sqrt{(22-10)^2 + (4+6)^2} = \sqrt{12^2 + 10^2} = \sqrt{144 + 100} = \sqrt{244} = 2\sqrt{61}$ units OR It is given that P (x,y) is equidistant from A(3, 6) and B(-3, 4). Using Distance formula, we can write PA = PB $\sqrt{(x-3)^2+(y-6)^2} = \sqrt{[x-(-3)]^2+(y-4)^2}$ $\Rightarrow \sqrt{x^2 + 9 - 6x + y^2 + 36 - 12y} = \sqrt{x^2 + 9 + 6x + y^2 + 16 - 8y}$ Squaring both sides, we get $\Rightarrow x^2 + 9 - 6x + y^2 + 36 - 12y = x^2 + 9 + 6x + y^2 + 16 - 8y$ $\Rightarrow -6x - 12y + 45 = 6x - 8y + 25$ \Rightarrow 12x + 4y = 20 \Rightarrow 3x + y = 5 23. The quadratic equation is given as: $4u^2 + 8u$ it can be written in the standard form as: $=4u^2 + 8u + 0$ = 4u(u + 2)The value of $4u^2 + 8u$ is zero when 4u = 0 or u + 2 = 0, i.e., u = 0 or u = -2Therefore, the zeroes of $4u^2 + 8u$ are 0 and -2Sum of zeroes = $0 + (-2) = -2 = \frac{-(8)}{4} = \frac{-(\text{ coefficient of } u)}{\text{coefficient of } u^2}$ Product of zeroes = $0 \times (-2) = 0 = \frac{0}{4} = \frac{\text{constant torm}}{\text{coefficient of } u^2}$ Hence verified С S R 24. O B

Steps of construction:

(i) Draw a line segment PQ of 14 cm.

(ii) Take the midpoint O of PQ.

(iii) Draw the perpendicular bisectors of PO and OQ which intersects at points R and S.

(iv) With center R and radius RP draw a circle.

(v) With center S and radius, SQ draw a circle.

(vi) With center O and radius 3 cm draw another circle which intersects the previous circles at the points A, B, C, and D.

(vii) Join PA, PB, QC, and QD.

So, PA, PB, QC, and QD are the required tangents.

25.
$$\sin 60^{\circ} \cos 30^{\circ} + \sin 30^{\circ} \cos 60^{\circ}$$

= $\frac{\sqrt{3}}{2} \cdot \frac{\sqrt{3}}{2} + \frac{1}{2} \cdot \frac{1}{2}$
= $\frac{3}{4} + \frac{1}{4} = 1$

OR

LHS

$$= \frac{\sin \theta - 2 \sin^3 \theta}{2 \cos^2 \theta - \cos \theta} = \frac{\sin \theta (1 - 2 \sin^2 \theta)}{\cos \theta (2 \cos^2 \theta - 1)}$$

$$= \frac{\sin \theta (\cos^2 \theta + \sin^2 \theta - 2 \sin^2 \theta)}{\cos \theta (2 \cos^2 \theta - \cos^2 \theta - \sin^2 \theta)} \quad \because \cos^2 \theta + \sin^2 \theta = 1$$

$$= \frac{\sin \theta (\cos^2 \theta - \sin^2 \theta)}{\cos \theta (\cos^2 \theta - \sin^2 \theta)} = \tan \theta$$
= RHS

In larger circle C1, AB is the chord and OP is the tangent. Therefore, $\angle OPB = 90^{\circ}$

Hence, AP = PB (perpendicular from center of the circle to the chord bisects the chord)

27. We can prove $7\sqrt{5}$ irrational by contradiction.

Let us suppose that $7\sqrt{5}$ is rational.

It means we have some co-prime integers *a* and *b* ($b \neq 0$) such that

$$7\sqrt{5} = \frac{a}{b}$$

 $\Rightarrow \sqrt{5} = \frac{a}{7b}$ (1)

R.H.S of (1) is rational but we know that $\sqrt{5}$ is irrational. It is not possible which means our supposition is wrong. Therefore, $7\sqrt{5}$ cannot be rational. Hence, it is irrational.

28. Let the two consecutive odd positive integers be 'x' & 'x + 2'. According to the question :-

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x^2 + (x + 2)^2 = 290
\Rightarrow 2x^2 + 4x + 4 = 290
\Rightarrow 2x^2 + 4x - 286 = 0
\Rightarrow x<sup>2</sup> + 2x - 143 = 0
\Rightarrow x<sup>2</sup> + 13x - 11x - 143 = 0
\Rightarrow x(x + 13) - 11(x + 13) = 0
\Rightarrow (x + 13) (x - 11) = 0
\Rightarrow x - 11 = 0 [\therefore x > 0 \therefore x + 13 \neq 0]
\Rightarrow x = 11 & so, x + 2 = 13
Hence, required consecutive odd positive integers are 11 and 13.
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Let the base of the right triangle be x cm. Then altitude = (x - 7) cm Hypotenuse = 13 cm By Pythagoras theorem $(Base)^2 + (Altitude)^2 = (Hypotenuse)^2$ $\implies x^2 + (x-7)^2 = (13)^2$ $\implies x^2 + x^2 - 14x + 49 = 169$ $\implies 2x^2 - 14x - 120 = 0$ \implies 2(x² - 7x -60) = 0 or x² - 7x -60 = 0 \implies x² - 12x + 5x -60 = 0 \implies x (x - 12) +5 (x - 12) = 0 \implies (x + 5) (x - 12) = 0 Either x + 5 = 0 or x - 12 = 0Since side of the triangle cannot be negative. So, x = 12 cm and x = -5 is rejected. Hence, length of the other two sides are 12cm, (12 - 7) = 5cm. $= \frac{1}{3}(21y^2 - 14y + 3y - 2)$ $= \frac{1}{3} [7y(3y - 2) + 1(3y - 2)]$ $\Rightarrow y = \frac{2}{3}, \frac{-1}{7}$ are zeroes of the polynomial. If Given polynimoal is $7y^2 - \frac{11}{3}y - \frac{2}{3}$ Then a = 7, b = $-\frac{11}{3}$ and c = $-\frac{2}{3}$ Sum of zeroes = $\frac{2}{3} + \frac{-1}{7} = \frac{14-3}{21} = \frac{11}{21}$ (i)

30. We know that, the sum of three angles of a triangle is 180⁰.

Now, product of zeroes = $\frac{2}{3} \times \frac{-1}{7} = \frac{-2}{21}$ (iii)

In \triangle PQR, \angle P + \angle Q + \angle R = 180° \Rightarrow 55^o + 25^o + $\angle R$ = 180^o $\Rightarrow \angle R = 180^{\circ} - (55^{\circ} + 25^{\circ}) = 180^{\circ} - 80^{\circ} = 100^{\circ}$ In \triangle TSM, \angle T + \angle S + \angle M = 180^o $\Rightarrow \angle T + \angle 25^{\circ} + 1000^{\circ} = 180^{\circ}$ $\Rightarrow \angle T = 180^{\circ} - (25^{\circ} + 100^{\circ})$ $= 180^{\circ} - 125^{\circ} = 55^{\circ}$ 25°

In \triangle PQR and \triangle TSM, we have

⇒ x = -5, 12

 $=\frac{1}{3}(21y^2 - 11y - 2)$

 $=\frac{1}{3}(3y-2)(7y+1)$

From (i) and (ii) Sum of zeroes = $\frac{-b}{a}$

From (iii) and (iv) Product of zeroes = $\frac{c}{a}$

Also, $\frac{-b}{a} = \frac{-\left(\frac{-11}{3}\right)}{7} = \frac{11}{21}$ (ii)

Also, $\frac{c}{a} = \frac{\frac{-2}{3}}{7} = \frac{-2}{21}$ (iv)

29. $7y^2 - \frac{11}{3}y - \frac{2}{3}$

 $\angle P = \angle T, \angle Q = \angle S,$ and $\angle R = \angle M$ Therefore, $\triangle PQR \sim \triangle TSM$ [since, all corresponding angles are equal] Hence, $\triangle QPR$ is not similar to $\triangle TSM$, since correct correspondence is $P \leftrightarrow T, Q < r \leftrightarrow S$ and $R \leftrightarrow M$.

OR



Distance traveled by the plane flying toward north in $1\frac{1}{2}$ hrs

 $=1,000 imes 1rac{1}{2}=1,500 km$

Similarly, distance traveled by the plane flying towards west in $1\frac{1}{2}$ hrs

 $=1,200 imes 1rac{1}{2}=1,800 km$

Let these distances are represented by OA and OB respectively. Now applying Pythagoras theorem

Distance between these planes after $1\frac{1}{2}$ hrs $AB = \sqrt{OA^2 + OB^2}$

 $=\sqrt{\left(1,500
ight)^2+\left(1,800
ight)^2}=\sqrt{2250000+3240000}$

 $=\sqrt{5490000}=\sqrt{9 imes 610000}=300\sqrt{61}$

So, distance between these planes will be $300\sqrt{61}$ km, after $1\frac{1}{2}$ hrs.

31. According to the question, A child's game has 8 triangles of which 3 are blue and rest are red, and 10 squares of which 6 are blue and rest are red.

Total number of pieces =8+10=18

i. No. of triangles = 8.

Hence, P(triangle is lost) = $\frac{8}{18} = \frac{4}{9}$

- ii. No. of squares = 10 Hence, P(square is lost) = $\frac{10}{18} = \frac{5}{9}$
- iii. No. of squares of blue colour = 6. So, P(square of blue colour is lost) = $\frac{6}{18} = \frac{1}{3}$
- iv. No. of triangles of red colour = $8 \frac{3}{5} = 5$
 - So, P(triangle of red colour is lost) = $\frac{5}{18}$

32. In right triangle ABQ,

(Top) A

$$\int_{75 \text{ m}}^{30^{\circ}} \int_{45^{\circ}}^{45^{\circ}} \int_{9}^{75 \text{ m}} \int_{9}^{10^{\circ}} \int_{9}^{45^{\circ}} \int_{9}^{10^{\circ}} \int_{10^{\circ}}^{10^{\circ}} \int_{10^$$

 $QP = 75(\sqrt{3} - 1) m$

Hence the distance between the two ships is $75(\sqrt{3}-1)$ m.

33. We first find the class mark x_i, of each class and then proceed as follows

Weight (in kg)	Number of wrestles (f _i)	Class Marks (x _i)	Deviation d _i = x _i - a	$f_i d_i$
100-110	4	105	-20	-80
110-120	14	115	-10	-140
120-130	21	a=125	0	0
130-140	8	135	10	80
140-150	3	145	20	60
		$N=\sum f_i=50$		$\sum f_i d_i = -80$

: Assumed mean, (a) = 125 Class width, (h) = 10and total observations, (N) = 50 By step deviation method, $ext{Mean}\left(ar{x}
ight)=a+rac{\sum f_{d}d}{\sum f_{i}} \ ext{Mean}\left(ar{x}
ight)=125+rac{(-80)}{50} \ ext{}$ = 125 - 16 = 123.4kg Hence, mean weight of wrestlers = 123.4kg 34. $\angle C = 3 \angle B = 2(\angle A + \angle B)$ Taking 3 $\angle B$ = 2($\angle A$ + $\angle B$) $\Rightarrow \angle B = 2 \angle A$ $\Rightarrow 2 \angle A - \angle B = 0 \dots (1)$ We know that the sum of the measures of all angles of a triangle is 180°. $\angle A + \angle B + \angle C = 180^{\circ}$ $\Rightarrow \angle A + \angle B + 3 \angle B = 180^{\circ}$ $\Rightarrow \angle A + 4 \angle B = 180^{\circ}$ (2) Multiplying equation (1) by 4, we obtain: $8 \angle A - 4 \angle B = 0 \dots (3)$ Adding equations (2) and (3), we get 9 ∠A = 180° ⇒∠A = 20° From eq. (2), we get, 20° + 4 ∠B = 180° $\Rightarrow \angle B = 40^{\circ}$ And $\angle C = 3 \ge 40^\circ = 120^\circ$ Hence the measures of $\angle A$, $\angle B$ and $\angle C$ are 20°, 40° and 120° respectively.

OR

i. By Elimination method The given system of equation is $\frac{x}{2} + \frac{2y}{3} = -1$(1) $x - \frac{y}{3} = 3$(2) Multiplying equation (2) by 2, we get $2x - \frac{2y}{3} = 6$(3) Adding equation(1) and equation (2), we get $\frac{5}{2}x = 5 \Rightarrow x = \frac{5 \times 2}{5} \Rightarrow x = 2$ Substituting this value of x in equation(2), we get $2 - \frac{y}{3} = 3 \Rightarrow \frac{y}{3} = 2 - 3 = -1 \Rightarrow y = -3$ So, the solution of the given system of equation is x = 2, y = -3

ii. By substitution method

The given system of equation is

The given system of equation is

$$\frac{x}{2} + \frac{2y}{3} = -1.....(1)$$

$$x - \frac{y}{3} = 3.....(2)$$
From equation (2),

$$x = \frac{y}{3} + 3.....(3)$$
Substituting this value of x in (1),

$$\frac{1}{2}\left(\frac{y}{3} + 3\right) + \frac{2y}{3} = -1$$

$$\Rightarrow \quad \frac{y}{6} + \frac{3}{2} + \frac{2y}{3} = -1 \Rightarrow \quad \frac{5y}{6} = -1 - \frac{3}{2}$$

$$\Rightarrow \quad \frac{5y}{6} - -\frac{5}{2} \Rightarrow y = -3$$
Substituting this value of y in equation (3), we get

$$x = -\frac{3}{3} + 3 = -1 + 3 - 2$$
So, the solution of the given system of equations is x = 2, y = -3

Verification: Substituting x = 2, y = -3, we find that both the equation (1) and (2) are satisfied as shown below:

$$\frac{x}{2} + \frac{2y}{3} = \frac{2}{2} + \frac{2(-3)}{3} = 1 - 2 = -1$$

35. Area of minor segment = Area of sector – Area of \triangle OAB

12 imes12

 $(75.36 - 36\sqrt{3}) \text{ cm}^2.$

In $\triangle OAB$,

$$\theta = 60^{\circ}$$

$$OA = OB = r = 12 \text{ cm}$$

$$\angle B = \angle A = x [\angle s \text{ opp. to equal sides are equal}]$$

$$\Rightarrow \angle A + \angle B + \angle O = 180^{\circ}$$

$$\Rightarrow x + x + 60^{\circ} = 180^{\circ}$$

$$\Rightarrow 2x = 180^{\circ} - 60^{\circ}$$

$$\Rightarrow x = \frac{120^{\circ}}{2} = 60^{\circ}$$

$$\therefore \triangle OAB \text{ is equilateral } \triangle \text{ with each side (a) = 12 cm}$$
Area of the equilateral $\triangle = \frac{\sqrt{3}}{4}a^{2}$
Area of minor segment = Area of the sector – Area of $\triangle OAB$

$$= \frac{\pi r^{2}\theta}{360^{\circ}} - \frac{\sqrt{3}}{4}a^{2}$$

$$= \frac{3.14 \times 12 \times 12 \times 60^{\circ}}{360^{\circ}} - \frac{\sqrt{3}}{4} \times 12 \times 12$$

$$= 6.28 \times 12 - 36\sqrt{3}$$

$$\therefore \text{ Area of minor segment = (75.36 - 36\sqrt{3}) cm^{2}.$$
36.
$$Area of minor segment = (75.36 - 36\sqrt{3}) cm^{2}.$$
Let BC be the building, AB be the transmission tower, and D

be the transmission tower, and D be the point on the ground.

In
$$\triangle BCD$$
,
 $\frac{BC}{CD} = tan45^{\circ}$
 $\Rightarrow \frac{20}{CD} = 1$
 $\Rightarrow CD = 20$
In $\triangle ACD$,
 $\frac{AC}{CD} = tan60^{\circ}$
 $\Rightarrow \frac{AB+BC}{CD} = \sqrt{3}$
 $\Rightarrow \frac{AB+20}{20} = \sqrt{3}$
 $\Rightarrow AB + 20 = 20\sqrt{3}$
 $\Rightarrow AB = 20(\sqrt{3} - 1) m$.